Review Problems

1-85 A hydraulic lift is used to lift a weight. The diameter of the piston on which the weight to be placed is to be determined.

**Assumptions** 1 The cylinders of the lift are vertical. 2 There are no leaks. 3 Atmospheric pressure act on both sides, and thus it can be disregarded.

**Analysis** Noting that pressure is force per unit area, the pressure on the smaller piston is determined from

\[
P = \frac{F_1}{A_1} = \frac{m g}{\pi D_1^2 / 4}
\]

\[
= \frac{(25 \text{ kg})(9.81 \text{ m/s}^2)}{\pi(0.10 \text{ m})^2 / 4} \left( \frac{1 \text{ kN}}{1000 \text{ kg} \cdot \text{m/s}^2} \right)
\]

\[
= 31.23 \text{ kN/m}^2 = 31.23 \text{ kPa}
\]

From Pascal’s principle, the pressure on the greater piston is equal to that in the smaller piston. Then, the needed diameter is determined from

\[
P_1 = P_2 = \frac{F_2}{A_2} = \frac{m_2 g}{\pi D_2^2 / 4} \longrightarrow 31.23 \text{ kN/m}^2 = \frac{(2500 \text{ kg})(9.81 \text{ m/s}^2)}{\pi D_2^2 / 4} \left( \frac{1 \text{ kN}}{1000 \text{ kg} \cdot \text{m/s}^2} \right) \longrightarrow D_2 = 1.0 \text{ m}
\]

**Discussion** Note that large weights can be raised by little effort in hydraulic lift by making use of Pascal’s principle.

1-86 A vertical piston-cylinder device contains a gas. Some weights are to be placed on the piston to increase the gas pressure. The local atmospheric pressure and the mass of the weights that will double the pressure of the gas are to be determined.

**Assumptions** Friction between the piston and the cylinder is negligible.

**Analysis** The gas pressure in the piston-cylinder device initially depends on the local atmospheric pressure and the weight of the piston. Balancing the vertical forces yield

\[
P_{\text{atm}} = P - \frac{m_{\text{piston}} g}{A} = 100 \text{ kPa} - \frac{(5 \text{ kg})(9.81 \text{ m/s}^2)}{\pi(0.12 \text{ m}^2)/4} \left( \frac{1 \text{ kN}}{1000 \text{ kg} \cdot \text{m/s}^2} \right) = 95.66 \text{ kN/m}^2 = 95.7 \text{ kPa}
\]

The force balance when the weights are placed is used to determine the mass of the weights

\[
P = P_{\text{atm}} + \frac{(m_{\text{piston}} + m_{\text{weights}}) g}{A}
\]

\[
200 \text{ kPa} = 95.66 \text{ kPa} + \frac{(5 \text{ kg} + m_{\text{weights}})(9.81 \text{ m/s}^2)}{\pi(0.12 \text{ m}^2)/4} \left( \frac{1 \text{ kN}}{1000 \text{ kg} \cdot \text{m/s}^2} \right) \longrightarrow m_{\text{weights}} = 115.3 \text{ kg}
\]

A large mass is needed to double the pressure.
An airplane is flying over a city. The local atmospheric pressure in that city is to be determined.

**Assumptions** The gravitational acceleration does not change with altitude.

**Properties** The densities of air and mercury are given to be 1.15 kg/m\(^3\) and 13,600 kg/m\(^3\).

**Analysis** The local atmospheric pressure is determined from

\[
P_{\text{atm}} = P_{\text{plane}} + \rho g h
\]

\[
= 58 \text{kPa} + (1.15 \text{ kg/m}^3)(9.81 \text{ m/s}^2)(3000 \text{ m})
\left(\frac{1 \text{kN}}{1000 \text{ kg} \cdot \text{m/s}^2}\right)
= 91.84 \text{kN/m}^2
= 91.8 \text{kPa}
\]

The atmospheric pressure may be expressed in mmHg as

\[
h_{\text{Hg}} = \frac{P_{\text{atm}}}{\rho g} = \frac{91.8 \text{kPa}}{(13,600 \text{ kg/m}^3)(9.81 \text{ m/s}^2)}
\left(\frac{1000 \text{ Pa}}{1 \text{kPa}}\right)
\left(\frac{1000 \text{ mm}}{1 \text{ m}}\right)
= 688 \text{ mmHg}
\]

The gravitational acceleration changes with altitude. Accounting for this variation, the weights of a body at different locations are to be determined.

**Analysis** The weight of an 80-kg man at various locations is obtained by substituting the altitude \(z\) (values in m) into the relation

\[
W = mg = (80 \text{ kg})(9.807 - 3.32 \times 10^{-6} \times z \text{ m/s}^2)
\left(\frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2}\right)
\]

Sea level: \((z = 0 \text{ m})\): \(W = 80 \times (9.807 - 3.32 \times 10^{-6} \times 0) = 80 \times 9.807 = 784.6 \text{ N}\)

Denver: \((z = 1610 \text{ m})\): \(W = 80 \times (9.807 - 3.32 \times 10^{-6} \times 1610) = 80 \times 9.802 = 784.2 \text{ N}\)

Mt. Ev.: \((z = 8848 \text{ m})\): \(W = 80 \times (9.807 - 3.32 \times 10^{-6} \times 8848) = 80 \times 9.778 = 782.2 \text{ N}\)

A man is considering buying a 12-oz steak for $3.15, or a 320-g steak for $2.80. The steak that is a better buy is to be determined.

**Assumptions** The steaks are of identical quality.

**Analysis** To make a comparison possible, we need to express the cost of each steak on a common basis. Let us choose 1 kg as the basis for comparison. Using proper conversion factors, the unit cost of each steak is determined to be

12 ounce steak: Unit Cost = \($3.15 \div 16 \text{ oz}) \left(\frac{1 \text{ lbm}}{1 \text{ lbm}}\right) \left(\frac{1 \text{ lbm}}{0.45359 \text{ kg}}\right) = $9.26/\text{kg}\)

320 gram steak:

Unit Cost = \($2.80 \div 320 \text{ g}) \left(\frac{1000 \text{ g}}{1 \text{ kg}}\right) = $8.75/\text{kg}\)

Therefore, the steak at the international market is a better buy.
1-90 The thrust developed by the jet engine of a Boeing 777 is given to be 85,000 pounds. This thrust is to be expressed in N and kgf.

**Analysis** Noting that 1 lbf = 4.448 N and 1 kgf = 9.81 N, the thrust developed can be expressed in two other units as

\[
\text{Thrust in N: } \quad \text{Thrust} = (85,000 \text{ lbf}) \left(\frac{4.448 \text{ N}}{1 \text{ lbf}}\right) = 3.78 \times 10^5 \text{ N}
\]

\[
\text{Thrust in kgf: } \quad \text{Thrust} = (37.8 \times 10^5 \text{ N}) \left(\frac{1 \text{ kgf}}{9.81 \text{ N}}\right) = 3.85 \times 10^4 \text{ kgf}
\]

1-91E The efficiency of a refrigerator increases by 3% per °C rise in the minimum temperature. This increase is to be expressed per °F, K, and R rise in the minimum temperature.

**Analysis** The magnitudes of 1 K and 1°C are identical, so are the magnitudes of 1 R and 1°F. Also, a change of 1 K or 1°C in temperature corresponds to a change of 1.8 R or 1.8°F. Therefore, the increase in efficiency is

(a) 3% for each K rise in temperature, and
(b), (c) \( \frac{3}{1.8} = 1.67\% \) for each R or °F rise in temperature.

1-92E The boiling temperature of water decreases by 3°C for each 1000 m rise in altitude. This decrease in temperature is to be expressed in °F, K, and R.

**Analysis** The magnitudes of 1 K and 1°C are identical, so are the magnitudes of 1 R and 1°F. Also, a change of 1 K or 1°C in temperature corresponds to a change of 1.8 R or 1.8°F. Therefore, the decrease in the boiling temperature is

(a) 3 K for each 1000 m rise in altitude, and
(b), (c) \( 3 \times 1.8 = 5.4 \text{°F} = 5.4 \text{ R} \) for each 1000 m rise in altitude.

1-93E The average body temperature of a person rises by about 2°C during strenuous exercise. This increase in temperature is to be expressed in °F, K, and R.

**Analysis** The magnitudes of 1 K and 1°C are identical, so are the magnitudes of 1 R and 1°F. Also, a change of 1 K or 1°C in temperature corresponds to a change of 1.8 R or 1.8°F. Therefore, the rise in the body temperature during strenuous exercise is

(a) 2 K
(b) \( 2 \times 1.8 = 3.6 \text{°F} \)
(c) \( 2 \times 1.8 = 3.6 \text{ R} \)
Hyperthermia of 5°C is considered fatal. This fatal level temperature change of body temperature is to be expressed in °F, K, and R.

**Analysis** The magnitudes of 1 K and 1°C are identical, so are the magnitudes of 1 R and 1°F. Also, a change of 1 K or 1°C in temperature corresponds to a change of 1.8 R or 1.8°F. Therefore, the fatal level of hypothermia is

(a) 5 K
(b) 5×1.8 = 9°F
(c) 5×1.8 = 9 R

A house is losing heat at a rate of 4500 kJ/h per °C temperature difference between the indoor and the outdoor temperatures. The rate of heat loss is to be expressed per °F, K, and R of temperature difference between the indoor and the outdoor temperatures.

**Analysis** The magnitudes of 1 K and 1°C are identical, so are the magnitudes of 1 R and 1°F. Also, a change of 1 K or 1°C in temperature corresponds to a change of 1.8 R or 1.8°F. Therefore, the rate of heat loss from the house is

(a) 4500 kJ/h per K difference in temperature, and
(b), (c) 4500/1.8 = 2500 kJ/h per R or °F rise in temperature.

The average temperature of the atmosphere is expressed as $T_{\text{atm}} = 288.15 - 6.5z$ where $z$ is altitude in km. The temperature outside an airplane cruising at 12,000 m is to be determined.

**Analysis** Using the relation given, the average temperature of the atmosphere at an altitude of 12,000 m is determined to be

$$T_{\text{atm}} = 288.15 - 6.5z$$
$$= 288.15 - 6.5 \times 12$$
$$= 210.15 \text{ K} = -63\degree \text{C}$$

**Discussion** This is the “average” temperature. The actual temperature at different times can be different.

A new “Smith” absolute temperature scale is proposed, and a value of 1000 S is assigned to the boiling point of water. The ice point on this scale, and its relation to the Kelvin scale are to be determined.

**Analysis** All linear absolute temperature scales read zero at absolute zero pressure, and are constant multiples of each other. For example, $T(R) = 1.8 \times T(K)$. That is, multiplying a temperature value in K by 1.8 will give the same temperature in R.

The proposed temperature scale is an acceptable absolute temperature scale since it differs from the other absolute temperature scales by a constant only. The boiling temperature of water in the Kelvin and the Smith scales are 315.15 K and 1000 K, respectively. Therefore, these two temperature scales are related to each other by

$$T(S) = \frac{1000}{373.15} \times T(K) = 2.6799 \times T(K)$$

The ice point of water on the Smith scale is

$$T(S)_{\text{ice}} = 2.6799 \times T(K)_{\text{ice}} = 2.6799 \times 273.15 = 732.0 \text{ S}$$
An expression for the equivalent wind chill temperature is given in English units. It is to be converted to SI units.

**Analysis** The required conversion relations are \( 1 \text{ mph} = 1.609 \text{ km/h} \) and \( T(\circ F) = 1.8T(\circ C) + 32 \). The first thought that comes to mind is to replace \( T(\circ F) \) in the equation by its equivalent \( 1.8T(\circ C) + 32 \), and \( V \) in mph by 1.609 km/h, which is the “regular” way of converting units. However, the equation we have is not a regular dimensionally homogeneous equation, and thus the regular rules do not apply. The \( V \) in the equation is a constant whose value is equal to the numerical value of the velocity in mph. Therefore, if \( V \) is given in km/h, we should divide it by 1.609 to convert it to the desired unit of mph. That is,

\[
T_{\text{equiv}}(\circ F) = 91.4 - [91.4 - T_{\text{ambient}}(\circ F)][0.475 - 0.0203(V/1.609) + 0.304\sqrt{V}/1.609]
\]

or

\[
T_{\text{equiv}}(\circ F) = 91.4 - [91.4 - T_{\text{ambient}}(\circ F)][0.475 - 0.0126V + 0.240\sqrt{V}]
\]

where \( V \) is in km/h. Now the problem reduces to converting a temperature in \( \circ F \) to a temperature in \( \circ C \), using the proper convection relation:

\[
1.8T_{\text{equiv}}(\circ C) + 32 = 91.4 - [91.4 - (1.8T_{\text{ambient}}(\circ C) + 32)][0.475 - 0.0126V + 0.240\sqrt{V}]
\]

which simplifies to

\[
T_{\text{equiv}}(\circ C) = 33.0 - (33.0 - T_{\text{ambient}})(0.475 - 0.0126V + 0.240\sqrt{V})
\]

where the ambient air temperature is in \( \circ C \).
**1-99E EES** Problem 1-98E is reconsidered. The equivalent wind-chill temperatures in °F as a function of wind velocity in the range of 4 mph to 100 mph for the ambient temperatures of 20, 40, and 60°F are to be plotted, and the results are to be discussed.

**Analysis** The problem is solved using EES, and the solution is given below.

"Obtain V and T_ambient from the Diagram Window"

(T_ambient=10
V=20)

V_use=max(V,4)

T_equiv=91.4-(91.4-T_ambient)*(0.475 - 0.0203*V_use + 0.304*sqrt(V_use))

"The parametric table was used to generate the plot. Fill in values for T_ambient and V (use Alter Values under Tables menu) then use F3 to solve table. Plot the first 10 rows and then overlay the second ten, and so on. Place the text on the plot using Add Text under the Plot menu."

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<th>V [mph]</th>
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1-100 One section of the duct of an air-conditioning system is laid underwater. The upward force the water will exert on the duct is to be determined.

**Assumptions**
1. The diameter given is the outer diameter of the duct (or, the thickness of the duct material is negligible).
2. The weight of the duct and the air in is negligible.

**Properties**
The density of air is given to be \( \rho = 1.30 \text{ kg/m}^3 \). We take the density of water to be 1000 kg/m\(^3\).

**Analysis**
Noting that the weight of the duct and the air in it is negligible, the net upward force acting on the duct is the buoyancy force exerted by water. The volume of the underground section of the duct is

\[
V = AL = (\pi D^2 / 4)L = [\pi(0.15 \text{ m})^2 / 4](20 \text{ m}) = 0.353 \text{ m}^3
\]

Then the buoyancy force becomes

\[
F_B = \rho g V = (1000 \text{ kg/m}^3)(9.81 \text{ m/s}^2)(0.353 \text{ m}^3) \left( \frac{1 \text{ kN}}{1000 \text{ kg} \cdot \text{m/s}^2} \right) = 3.46 \text{ kN}
\]

**Discussion**
The upward force exerted by water on the duct is 3.46 kN, which is equivalent to the weight of a mass of 353 kg. Therefore, this force must be treated seriously.

1-101 A helium balloon tied to the ground carries 2 people. The acceleration of the balloon when it is first released is to be determined.

**Assumptions**
The weight of the cage and the ropes of the balloon is negligible.

**Properties**
The density of air is given to be \( \rho = 1.16 \text{ kg/m}^3 \). The density of helium gas is \(1/7\) of this.

**Analysis**
The buoyancy force acting on the balloon is

\[
V_{balloon} = 4\pi r^3 / 3 = 4\pi(5 \text{ m})^3 / 3 = 523.6 \text{ m}^3
\]

\[
F_B = \rho \text{air} g V_{balloon}
= (1.16 \text{ kg/m}^3)(9.81 \text{ m/s}^2)(523.6 \text{ m}^3) \left( \frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2} \right) = 5958 \text{ N}
\]

The total mass is

\[
m_{He} = \rho_{He} V = \left( \frac{1.16}{7} \text{ kg/m}^3 \right)(523.6 \text{ m}^3) = 86.8 \text{ kg}
\]

\[
m_{total} = m_{He} + m_{people} = 86.8 + 2 \times 70 = 226.8 \text{ kg}
\]

The total weight is

\[
W = m_{total} g = (226.8 \text{ kg})(9.81 \text{ m/s}^2) \left( \frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2} \right) = 2225 \text{ N}
\]

Thus the net force acting on the balloon is

\[
F_{net} = F_B - W = 5958 - 2225 = 3733 \text{ N}
\]

Then the acceleration becomes

\[
a = \frac{F_{net}}{m_{total}} = \frac{3733 \text{ N}}{226.8 \text{ kg}} \left( \frac{1 \text{ kg} \cdot \text{m/s}^2}{1 \text{ N}} \right) = 16.5 \text{ m/s}^2
\]
Problem 1-101 is reconsidered. The effect of the number of people carried in the balloon on acceleration is to be investigated. Acceleration is to be plotted against the number of people, and the results are to be discussed.

**Analysis** The problem is solved using EES, and the solution is given below.

"Given Data:"

\[
\begin{align*}
\text{rho} \_ \text{air} &= 1.16 \text{[kg/m}^3]\text{] \quad \text{"density of air"} \\
g &= 9.807 \text{[m/s}^2]\text{]} \\
d \_ \text{balloon} &= 10 \text{[m]} \\
m \_ \text{1person} &= 70 \text{[kg]} \\
\end{align*}
\]

\{NoPeople = 2\} \text{ "Data supplied in Parametric Table"}

"Calculated values:"

\[
\begin{align*}
\text{rho} \_ \text{He} &= \text{rho} \_ \text{air}/7 \text{[kg/m}^3]\text{]} \quad \text{"density of helium"} \\
r \_ \text{balloon} &= d \_ \text{balloon}/2 \text{[m]} \\
V \_ \text{balloon} &= 4\pi r \_ \text{balloon}^3/3 \text{[m}^3]\text{]} \\
m \_ \text{people} &= \text{NoPeople} \times m \_ \text{1person} \text{[kg]} \\
m \_ \text{He} &= \text{rho} \_ \text{He} \times V \_ \text{balloon} \text{[kg]} \\
m \_ \text{total} &= m \_ \text{He} + m \_ \text{people} \text{[kg]} \\
\end{align*}
\]

"The total weight of balloon and people is:"

\[
W \_ \text{total} = m \_ \text{total} \times g \text{[N]}
\]

"The buoyancy force acting on the balloon, \(F\_b\), is equal to the weight of the air displaced by the balloon."

\[
F \_b = \text{rho} \_ \text{air} \times V \_ \text{balloon} \times g \text{[N]}
\]

"From the free body diagram of the balloon, the balancing vertical forces must equal the product of the total mass and the vertical acceleration:"

\[
F \_b - W \_\text{total} = m \_ \text{total} \times a \_ \text{up}
\]

<table>
<thead>
<tr>
<th>(a _ \text{up} \text{[m/s}^2])</th>
<th>NoPeople</th>
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\(a \_ \text{up} \text{[m/s}^2]\) vs NoPeople graph
A balloon is filled with helium gas. The maximum amount of load the balloon can carry is to be determined.

**Assumptions** The weight of the cage and the ropes of the balloon is negligible.

**Properties** The density of air is given to be $\rho = 1.16 \text{ kg/m}^3$. The density of helium gas is $1/7$th of this.

**Analysis** In the limiting case, the net force acting on the balloon will be zero. That is, the buoyancy force and the weight will balance each other:

$$W = mg = F_B$$

$$m_{\text{total}} = \frac{F_B}{g} = \frac{5958 \text{ N}}{9.81 \text{ m/s}^2} = 607.3 \text{ kg}$$

Thus,

$$m_{\text{people}} = m_{\text{total}} - m_{\text{He}} = 607.3 - 86.8 = \textbf{520.5 kg}$$

The pressure in a steam boiler is given in kgf/cm$^2$. It is to be expressed in psi, kPa, atm, and bars.

**Analysis** We note that $1 \text{ atm} = 1.03323 \text{ kgf/cm}^2$, $1 \text{ atm} = 14.696 \text{ psi}$, $1 \text{ atm} = 101.325 \text{ kPa}$, and $1 \text{ atm} = 1.01325 \text{ bar}$ (inner cover page of text). Then the desired conversions become:

**In atm:**

$$P = (92 \text{ kgf/cm}^2) \left( \frac{1 \text{ atm}}{1.03323 \text{ kgf/cm}^2} \right) = \textbf{89.04 atm}$$

**In psi:**

$$P = (92 \text{ kgf/cm}^2) \left( \frac{1 \text{ atm}}{1.03323 \text{ kgf/cm}^2} \right) \left( \frac{14.696 \text{ psi}}{1 \text{ atm}} \right) = \textbf{1309 psi}$$

**In kPa:**

$$P = (92 \text{ kgf/cm}^2) \left( \frac{1 \text{ atm}}{1.03323 \text{ kgf/cm}^2} \right) \left( \frac{101.325 \text{ kPa}}{1 \text{ atm}} \right) = \textbf{9022 kPa}$$

**In bars:**

$$P = (92 \text{ kgf/cm}^2) \left( \frac{1 \text{ atm}}{1.03323 \text{ kgf/cm}^2} \right) \left( \frac{1.01325 \text{ bar}}{1 \text{ atm}} \right) = \textbf{90.22 bar}$$

**Discussion** Note that the units atm, kgf/cm$^2$, and bar are almost identical to each other.
A barometer is used to measure the altitude of a plane relative to the ground. The barometric readings at the ground and in the plane are given. The altitude of the plane is to be determined.

**Assumptions** The variation of air density with altitude is negligible.

**Properties** The densities of air and mercury are given to be \( \rho = 1.20 \text{ kg/m}^3 \) and \( \rho = 13,600 \text{ kg/m}^3 \).

**Analysis** Atmospheric pressures at the location of the plane and the ground level are

\[
P_{\text{plane}} = (\rho g h)_{\text{plane}} = (13,600 \text{ kg/m}^3)(9.81 \text{ m/s}^2)(0.690 \text{ m}) \left( \frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2} \right) \left( \frac{1 \text{ kPa}}{1000 \text{ N/m}^2} \right) = 92.06 \text{ kPa}
\]

\[
P_{\text{ground}} = (\rho g h)_{\text{ground}} = (13,600 \text{ kg/m}^3)(9.81 \text{ m/s}^2)(0.753 \text{ m}) \left( \frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2} \right) \left( \frac{1 \text{ kPa}}{1000 \text{ N/m}^2} \right) = 100.46 \text{ kPa}
\]

Taking an air column between the airplane and the ground and writing a force balance per unit base area, we obtain

\[
\frac{W_{\text{air}}}{A} = P_{\text{ground}} - P_{\text{plane}} = (\rho g h)_{\text{air}} = P_{\text{ground}} - P_{\text{plane}}
\]

\[
(1.20 \text{ kg/m}^3)(9.81 \text{ m/s}^2)(h) \left( \frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2} \right) \left( \frac{1 \text{ kPa}}{1000 \text{ N/m}^2} \right) = (100.46 - 92.06) \text{ kPa}
\]

It yields \( h = 714 \text{ m} \), which is also the altitude of the airplane.

A 10-m high cylindrical container is filled with equal volumes of water and oil. The pressure difference between the top and the bottom of the container is to be determined.

**Properties** The density of water is given to be \( \rho = 1000 \text{ kg/m}^3 \). The specific gravity of oil is given to be 0.85.

**Analysis** The density of the oil is obtained by multiplying its specific gravity by the density of water,

\[
\rho = \text{SG} \times \rho_{\text{H}_2\text{O}} = (0.85)(1000 \text{ kg/m}^3) = 850 \text{ kg/m}^3
\]

The pressure difference between the top and the bottom of the cylinder is the sum of the pressure differences across the two fluids,

\[
\Delta P_{\text{total}} = \Delta P_{\text{oil}} + \Delta P_{\text{water}} = (\rho g h)_{\text{oil}} + (\rho g h)_{\text{water}}
\]

\[
= [(850 \text{ kg/m}^3)(9.81 \text{ m/s}^2)(5 \text{ m}) + (1000 \text{ kg/m}^3)(9.81 \text{ m/s}^2)(5 \text{ m})] \left( \frac{1 \text{ kPa}}{1000 \text{ N/m}^2} \right)
\]

\[
= 90.7 \text{ kPa}
\]
1-107 The pressure of a gas contained in a vertical piston-cylinder device is measured to be 250 kPa. The mass of the piston is to be determined.

**Assumptions** There is no friction between the piston and the cylinder.

**Analysis** Drawing the free body diagram of the piston and balancing the vertical forces yield

\[ W = P_A - P_{atm} A \]

\[ mg = (P - P_{atm}) A \]

\[ (m)(9.81 \text{ m/s}^2) = (250 - 100 \text{ kPa})(30 \times 10^{-4} \text{ m}^2) \left( \frac{1000 \text{ kg/m} \cdot \text{s}^2}{1 \text{kPa}} \right) \]

It yields \( m = 45.9 \text{ kg} \)

1-108 The gage pressure in a pressure cooker is maintained constant at 100 kPa by a petcock. The mass of the petcock is to be determined.

**Assumptions** There is no blockage of the pressure release valve.

**Analysis** Atmospheric pressure is acting on all surfaces of the petcock, which balances itself out. Therefore, it can be disregarded in calculations if we use the gage pressure as the cooker pressure. A force balance on the petcock (\( \Sigma F_y = 0 \)) yields

\[ W = P_{gage} A \]

\[ m = \frac{P_{gage} A}{g} = \frac{(100 \text{ kPa})(4 \times 10^{-6} \text{ m}^2)}{9.81 \text{ m/s}^2} \left( \frac{1000 \text{ kg/m} \cdot \text{s}^2}{1 \text{kPa}} \right) \]

\[ = 0.0408 \text{ kg} \]

1-109 A glass tube open to the atmosphere is attached to a water pipe, and the pressure at the bottom of the tube is measured. It is to be determined how high the water will rise in the tube.

**Properties** The density of water is given to be \( \rho = 1000 \text{ kg/m}^3 \).

**Analysis** The pressure at the bottom of the tube can be expressed as

\[ P = P_{atm} + (\rho g h)_{\text{tube}} \]

Solving for \( h \),

\[ h = \frac{P - P_{atm}}{\rho g} = \frac{(115 - 92) \text{ kPa}}{(1000 \text{ kg/m}^3)(9.81 \text{ m/s}^2)} \left( \frac{1 \text{ kg} \cdot \text{m/s}^2}{1 \text{ N}} \right) \left( \frac{1000 \text{ N/m}^2}{1 \text{kPa}} \right) \]

\[ = 2.34 \text{ m} \]
The average atmospheric pressure is given as $P_{\text{atm}} = 101.325(1 - 0.02256z)^{5.256}$ where $z$ is the altitude in km. The atmospheric pressures at various locations are to be determined.

**Analysis** The atmospheric pressures at various locations are obtained by substituting the altitude $z$ values in km into the relation

$$P_{\text{atm}} = 101.325(1 - 0.02256z)^{5.256}$$

- **Atlanta:** ($z = 0.306$ km): $P_{\text{atm}} = 101.325(1 - 0.02256 \times 0.306)^{5.256} = 97.7$ kPa
- **Denver:** ($z = 1.610$ km): $P_{\text{atm}} = 101.325(1 - 0.02256 \times 1.610)^{5.256} = 83.4$ kPa
- **M. City:** ($z = 2.309$ km): $P_{\text{atm}} = 101.325(1 - 0.02256 \times 2.309)^{5.256} = 76.5$ kPa
- **Mt. Ev.:** ($z = 8.848$ km): $P_{\text{atm}} = 101.325(1 - 0.02256 \times 8.848)^{5.256} = 31.4$ kPa

The air pressure in a duct is measured by an inclined manometer. For a given vertical level difference, the gage pressure in the duct and the length of the differential fluid column are to be determined.

**Assumptions** The manometer fluid is an incompressible substance.

**Properties** The density of the liquid is given to be $\rho = 0.81$ kg/L = 810 kg/m$^3$.

**Analysis** The gage pressure in the duct is determined from

$$P_{\text{gage}} = P_{\text{abs}} - P_{\text{atm}} = \rho gh$$

$$= (810 \text{ kg/m}^3)(9.81 \text{ m/s}^2)(0.08 \text{ m})$$

$$= 636 \text{ Pa}$$

The length of the differential fluid column is

$$L = \frac{h}{\sin \theta} = \frac{8 \text{ cm}}{\sin 35^\circ} = 13.9 \text{ cm}$$

**Discussion** Note that the length of the differential fluid column is extended considerably by inclining the manometer arm for better readability.

Equal volumes of water and oil are poured into a U-tube from different arms, and the oil side is pressurized until the contact surface of the two fluids moves to the bottom and the liquid levels in both arms become the same. The excess pressure applied on the oil side is to be determined.

**Assumptions** 1 Both water and oil are incompressible substances. 2 Oil does not mix with water. 3 The cross-sectional area of the U-tube is constant.

**Properties** The density of oil is given to be $\rho_{\text{oil}} = 49.3$ lbm/ft$^3$. We take the density of water to be $\rho_w = 62.4$ lbm/ft$^3$.

**Analysis** Noting that the pressure of both the water and the oil is the same at the contact surface, the pressure at this surface can be expressed as

$$P_{\text{contact}} = P_{\text{blow}} + \rho_a g h_a = P_{\text{atm}} + \rho_w g h_w$$

Noting that $h_a = h_w$ and rearranging,

$$P_{\text{gage, blow}} = P_{\text{blow}} - P_{\text{atm}} = (\rho_w - \rho_{\text{oil}}) gh$$

$$= (62.4 - 49.3 \text{ lbm/ft}^3)(32.2 \text{ ft/s}^2)(30/12 \text{ ft})$$

$$= 0.227 \text{ psi}$$

**Discussion** When the person stops blowing, the oil will rise and some water will flow into the right arm. It can be shown that when the curvature effects of the tube are disregarded, the differential height of water will be 23.7 in to balance 30-in of oil.
It is given that an IV fluid and the blood pressures balance each other when the bottle is at a certain height, and a certain gage pressure at the arm level is needed for sufficient flow rate. The gage pressure of the blood and elevation of the bottle required to maintain flow at the desired rate are to be determined.

**Assumptions** 1 The IV fluid is incompressible. 2 The IV bottle is open to the atmosphere.

**Properties** The density of the IV fluid is given to be \( \rho = 1020 \text{ kg/m}^3 \).

**Analysis**

\((a)\) Noting that the IV fluid and the blood pressures balance each other when the bottle is 1.2 m above the arm level, the gage pressure of the blood in the arm is simply equal to the gage pressure of the IV fluid at a depth of 1.2 m,

\[
P_{\text{gage, arm}} = P_{\text{abs}} - P_{\text{atm}} = \rho g h_{\text{arm-bottle}}
\]

\[
= (1020 \text{ kg/m}^3)(9.81 \text{ m/s}^2)(1.20 \text{ m}) \left( \frac{1 \text{ kN}}{1000 \text{ kg} \cdot \text{m/s}^2} \right) \left( \frac{1 \text{ kPa}}{1 \text{ kN/m}^2} \right)
\]

\[
= 12.0 \text{ kPa}
\]

\((b)\) To provide a gage pressure of 20 kPa at the arm level, the height of the bottle from the arm level is again determined from \( P_{\text{gage, arm}} = \rho g h_{\text{arm-bottle}} \) to be

\[
h_{\text{arm-bottle}} = \frac{P_{\text{gage, arm}}}{\rho g}
\]

\[
= \frac{20 \text{ kPa}}{(1020 \text{ kg/m}^3)(9.81 \text{ m/s}^2)} \left( \frac{1000 \text{ kg} \cdot \text{m/s}^2}{1 \text{ kN}} \right) \left( \frac{1 \text{ kPa}}{1 \text{ kN/m}^2} \right)
\]

\[
= 2.0 \text{ m}
\]

**Discussion** Note that the height of the reservoir can be used to control flow rates in gravity driven flows. When there is flow, the pressure drop in the tube due to friction should also be considered. This will result in raising the bottle a little higher to overcome pressure drop.
A gasoline line is connected to a pressure gage through a double-U manometer. For a given reading of the pressure gage, the gage pressure of the gasoline line is to be determined.

**Assumptions**
1. All the liquids are incompressible.
2. The effect of air column on pressure is negligible.

**Properties**
The specific gravities of oil, mercury, and gasoline are given to be 0.79, 13.6, and 0.70, respectively. We take the density of water to be $\rho_w = 1000 \text{ kg/m}^3$.

**Analysis**
Starting with the pressure indicated by the pressure gage and moving along the tube by adding (as we go down) or subtracting (as we go up) the $\rho gh$ terms until we reach the gasoline pipe, and setting the result equal to $P_{\text{gasoline}}$ gives

$$P_{\text{gage}} - \rho_w gh_w + \rho_{\text{oil}} gh_{\text{oil}} - \rho_{\text{Hg}} gh_{\text{Hg}} - \rho_{\text{gasoline}} gh_{\text{gasoline}} = P_{\text{gasoline}}$$

Rearranging,

$$P_{\text{gasoline}} = P_{\text{gage}} - \rho_w g(h_w - SG_{\text{oil}} h_{\text{oil}} + SG_{\text{Hg}} h_{\text{Hg}} + SG_{\text{gasoline}} h_{\text{gasoline}})$$

Substituting,

$$P_{\text{gasoline}} = 370 \text{ kPa} - (1000 \text{ kg/m}^3)(9.81 \text{ m/s}^2)\left[(0.45 \text{ m}) - 0.79(0.5 \text{ m}) + 13.6(0.1 \text{ m}) + 0.70(0.22 \text{ m})\right]$$

$$\times \left(\frac{1 \text{kN}}{1000 \text{ kg} \cdot \text{m/s}^2}\right)\left(\frac{1 \text{kPa}}{1 \text{kN/m}^2}\right)$$

$$= 354.6 \text{ kPa}$$

Therefore, the pressure in the gasoline pipe is 15.4 kPa lower than the pressure reading of the pressure gage.

**Discussion**
Note that sometimes the use of specific gravity offers great convenience in the solution of problems that involve several fluids.
A gasoline line is connected to a pressure gage through a double-U manometer. For a given reading of the pressure gage, the gage pressure of the gasoline line is to be determined.

**Assumptions**
1. All the liquids are incompressible.
2. The effect of air column on pressure is negligible.

**Properties**
The specific gravities of oil, mercury, and gasoline are given to be 0.79, 13.6, and 0.70, respectively. We take the density of water to be $\rho_w = 1000 \text{ kg/m}^3$.

**Analysis**
Starting with the pressure indicated by the pressure gage and moving along the tube by adding (as we go down) or subtracting (as we go up) the $\rho gh$ terms until we reach the gasoline pipe, and setting the result equal to $P_{\text{gasoline}}$ gives

$$P_{\text{gage}} - \rho_w gh_w + \rho_{\text{oil}} gh_{\text{oil}} - \rho_{\text{Hg}} gh_{\text{Hg}} - \rho_{\text{gasoline}} gh_{\text{gasoline}} = P_{\text{gasoline}}$$

Rearranging,

$$P_{\text{gasoline}} = P_{\text{gage}} - \rho_w g(h_w - SG_{\text{oil}} h_{\text{oil}} + SG_{\text{Hg}} h_{\text{Hg}} + SG_{\text{gasoline}} h_{\text{gasoline}})$$

Substituting,

$$P_{\text{gasoline}} = 180 \text{ kPa} - (1000 \text{ kg/m}^3)(9.807 \text{ m/s}^2)[(0.45 \text{ m}) - 0.79(0.5 \text{ m}) + 13.6(0.1 \text{ m}) + 0.70(0.22 \text{ m})]$$

$$\times \left( \frac{1 \text{ kN}}{1000 \text{ kg} \cdot \text{m/s}^2} \right) \left( \frac{1 \text{ kPa}}{1 \text{ kN/m}^2} \right)$$

$$= 164.6 \text{ kPa}$$

Therefore, the pressure in the gasoline pipe is 15.4 kPa lower than the pressure reading of the pressure gage.

**Discussion**
Note that sometimes the use of specific gravity offers great convenience in the solution of problems that involve several fluids.
**1-116E** A water pipe is connected to a double-U manometer whose free arm is open to the atmosphere. The absolute pressure at the center of the pipe is to be determined.

**Assumptions** 1 All the liquids are incompressible. 2 The solubility of the liquids in each other is negligible.

**Properties** The specific gravities of mercury and oil are given to be 13.6 and 0.80, respectively. We take the density of water to be \( \rho_w = 62.4 \text{ lbm/ft}^3 \).

**Analysis** Starting with the pressure at the center of the water pipe, and moving along the tube by adding (as we go down) or subtracting (as we go up) the \( \rho gh \) terms until we reach the free surface of oil where the oil tube is exposed to the atmosphere, and setting the result equal to \( P_{atm} \) gives

\[
P_{\text{water pipe}} - \rho_{\text{water}} gh_{\text{water}} + \rho_{\text{oil}} gh_{\text{oil}} - \rho_{\text{Hg}} gh_{\text{Hg}} - \rho_{\text{oil}} gh_{\text{oil}} = P_{atm}
\]

Solving for \( P_{\text{water pipe}} \),

\[
P_{\text{water pipe}} = P_{atm} + \rho_{\text{water}} g( h_{\text{water}} - SG_{\text{oil}} h_{\text{oil}} + SG_{\text{Hg}} h_{\text{Hg}} + SG_{\text{oil}} h_{\text{oil}} )
\]

Substituting,

\[
P_{\text{water pipe}} = 14.2 \text{ psia} + (62.4 \text{ lbm/ft}^3)(32.2 \text{ ft/s}^2)(35/12 \text{ ft}) - 0.8(60/12 \text{ ft}) + 13.6(15/12 \text{ ft})
\]

\[
+ 0.8(40/12 \text{ ft}) \times \left( \frac{1 \text{ lbf}}{32.2 \text{ lbm} \cdot \text{ft/s}^2} \right) \left( \frac{1 \text{ ft}^2}{144 \text{ in}^2} \right)
\]

\[
= 22.3 \text{ psia}
\]

Therefore, the absolute pressure in the water pipe is 22.3 psia.

**Discussion** Note that jumping horizontally from one tube to the next and realizing that pressure remains the same in the same fluid simplifies the analysis greatly.
The temperature of the atmosphere varies with altitude $z$ as $T = T_0 - \beta z$, while the gravitational acceleration varies by $g(z) = g_0 / (1 + z / 6,370,320)^2$. Relations for the variation of pressure in atmosphere are to be obtained (a) by ignoring and (b) by considering the variation of $g$ with altitude.

**Assumptions**
The air in the troposphere behaves as an ideal gas.

**Analysis** (a) Pressure change across a differential fluid layer of thickness $dz$ in the vertical $z$ direction is

$$dP = -\rho gdz$$

From the ideal gas relation, the air density can be expressed as $\rho = \frac{P}{RT} = \frac{P}{R(T_0 - \beta z)}$. Then,

$$dP = -\frac{P}{R(T_0 - \beta z)} gdz$$

Separating variables and integrating from $z = 0$ where $P = P_0$ to $z = z$ where $P = P$,

$$\int_{P_0}^{P} \frac{dP}{P} = -\int_{0}^{z} \frac{gdz}{R(T_0 - \beta z)}$$

Performing the integrations,

$$\ln \frac{P}{P_0} = \frac{g}{R\beta} \ln \frac{T_0 - \beta z}{T_0}$$

Rearranging, the desired relation for atmospheric pressure for the case of constant $g$ becomes

$$P = P_0 \left(1 - \frac{\beta z}{T_0}\right)^{\frac{g}{R\beta}}$$

(b) When the variation of $g$ with altitude is considered, the procedure remains the same but the expressions become more complicated,

$$dP = -\frac{P}{R(T_0 - \beta z)} \frac{g_0}{(1 + z / 6,370,320)^2} dz$$

Separating variables and integrating from $z = 0$ where $P = P_0$ to $z = z$ where $P = P$,

$$\int_{P_0}^{P} \frac{dP}{P} = -\int_{0}^{z} \frac{g_0 dz}{R(T_0 - \beta z)(1 + z / 6,370,320)^2}$$

Performing the integrations,

$$\ln P \bigg|_{P_0}^{P} = \frac{g_0}{R\beta} \left[\frac{1}{(1 + kT_0 / \beta)(1 + kz)} - \frac{1}{(1 + kT_0 / \beta)^2} \ln \frac{1 + kT_0 / \beta}{T_0 - \beta z}\right]$$

where $R = 287 \text{ J/kg·K} = 287 \text{ m}^2/\text{s}^2\cdot\text{K}$ is the gas constant of air. After some manipulations, we obtain

$$P = P_0 \exp \left[-\frac{g_0}{R(\beta + kT_0)} \left(\frac{1}{1 + 1/kz} - \frac{1}{1 + kT_0 / \beta} \ln \frac{1 + kT_0 / \beta}{T_0 - \beta z}\right)\right]$$

where $T_0 = 288.15 \text{ K}$, $\beta = 0.0065 \text{ K/m}$, $g_0 = 9.807 \text{ m/s}^2$, $k = 1/6,370,320 \text{ m}^{-1}$, and $z$ is the elevation in m.

**Discussion**

When performing the integration in part (b), the following expression from integral tables is used, together with a transformation of variable $x = T_0 - \beta z$,

$$\int \frac{dx}{x(a + bx)^2} = \frac{1}{a(a + bx)} - \frac{1}{a^2} \ln \frac{a + bx}{x}$$

Also, for $z = 11,000$ m, for example, the relations in (a) and (b) give 22.62 and 22.69 kPa, respectively.
The variation of pressure with density in a thick gas layer is given. A relation is to be obtained for pressure as a function of elevation \( z \).

**Assumptions** The property relation \( P = C \rho^n \) is valid over the entire region considered.

**Analysis** The pressure change across a differential fluid layer of thickness \( dz \) in the vertical \( z \) direction is given as,

\[
dP = -\rho g dz
\]

Also, the relation \( P = C \rho^n \) can be expressed as \( C = P / \rho^n = P_0 / \rho^n \), and thus

\[
\rho = \rho_0 (P / P_0)^{1/n}
\]

Substituting,

\[
dP = -g\rho_0 (P / P_0)^{1/n} dz
\]

Separating variables and integrating from \( z = 0 \) where \( P = P_0 = C \rho_0^n \) to \( z = z \) where \( P = P \),

\[
\int_{P_0}^{P} (P / P_0)^{-1/n} dP = -\rho_0 g \int_{0}^{z} dz
\]

Performing the integrations.

\[
P_0 \frac{(P / P_0)^{-1/n+1}}{-1/n+1} \bigg|_{P_0}^{P} = -\rho_0 g z \quad \rightarrow \quad \left( \frac{P}{P_0} \right)^{(n-1)/n} - 1 = -\frac{n-1}{n} \frac{\rho_0 g z}{P_0}
\]

Solving for \( P \),

\[
P = P_0 \left( 1 - \frac{n-1}{n} \frac{\rho_0 g z}{P_0} \right)^{n/(n-1)}
\]

which is the desired relation.

**Discussion** The final result could be expressed in various forms. The form given is very convenient for calculations as it facilitates unit cancellations and reduces the chance of error.
A pressure transducer is used to measure pressure by generating analogue signals, and it is to be calibrated by measuring both the pressure and the electric current simultaneously for various settings, and the results are tabulated. A calibration curve in the form of \( P = al + b \) is to be obtained, and the pressure corresponding to a signal of 10 mA is to be calculated.

**Assumptions**  Mercury is an incompressible liquid.

**Properties**  The specific gravity of mercury is given to be 13.56, and thus its density is 13,560 kg/m\(^3\).

**Analysis**  For a given differential height, the pressure can be calculated from

\[
P = \rho g \Delta h
\]

For \( \Delta h = 28.0 \text{ mm} = 0.0280 \text{ m} \), for example,

\[
P = 13.56(1000 \text{ kg/m}^3)(9.81 \text{ m/s}^2)(0.0280 \text{ m}) \left( \frac{1 \text{ kN}}{1000 \text{ kg} \cdot \text{m/s}^2} \right) \left( \frac{1 \text{ kPa}}{1 \text{ kN/m}^2} \right) = 3.75 \text{ kPa}
\]

Repeating the calculations and tabulating, we have

<table>
<thead>
<tr>
<th>( \Delta h ) (mm)</th>
<th>28.0</th>
<th>181.5</th>
<th>297.8</th>
<th>413.1</th>
<th>765.9</th>
<th>1027</th>
<th>1149</th>
<th>1362</th>
<th>1458</th>
<th>1536</th>
</tr>
</thead>
<tbody>
<tr>
<td>( P ) (kPa)</td>
<td>3.73</td>
<td>24.14</td>
<td>39.61</td>
<td>54.95</td>
<td>101.9</td>
<td>136.6</td>
<td>152.8</td>
<td>181.2</td>
<td>193.9</td>
<td>204.3</td>
</tr>
<tr>
<td>( I ) (mA)</td>
<td>4.21</td>
<td>5.78</td>
<td>6.97</td>
<td>8.15</td>
<td>11.76</td>
<td>14.43</td>
<td>15.68</td>
<td>17.86</td>
<td>18.84</td>
<td>19.64</td>
</tr>
</tbody>
</table>

A plot of \( P \) versus \( I \) is given below. It is clear that the pressure varies linearly with the current, and using EES, the best curve fit is obtained to be

\[
P = 13.00I - 51.00 \quad \text{(kPa)} \quad \text{for } 4.21 \leq I \leq 19.64.
\]

For \( I = 10 \text{ mA} \), for example, we would get \( P = 79.0 \text{ kPa} \).

**Discussion**  Note that the calibration relation is valid in the specified range of currents or pressures.
Fundamentals of Engineering (FE) Exam Problems

**1-120** Consider a fish swimming 5 m below the free surface of water. The increase in the pressure exerted on the fish when it dives to a depth of 45 m below the free surface is

(a) 392 Pa 
(b) 9800 Pa  
(c) 50,000 Pa  
(d) 392,000 Pa  
(e) 441,000 Pa

*Answer* (d) 392,000 Pa

**Solution** Solved by EES Software. Solutions can be verified by copying-and-pasting the following lines on a blank EES screen. (Similar problems and their solutions can be obtained easily by modifying numerical values).

\[
\begin{align*}
\rho &= 1000 \text{ kg/m}^3 \\
g &= 9.81 \text{ m/s}^2 \\
z_1 &= 5 \text{ m} \\
z_2 &= 45 \text{ m} \\
\Delta P &= \rho g (z_2 - z_1) \text{ Pa}
\end{align*}
\]

"Some Wrong Solutions with Common Mistakes:"  
W1_P = \rho g (z_2 - z_1) / 1000 "dividing by 1000"  
W2_P = \rho g (z_1 + z_2) "adding depths instead of subtracting"  
W3_P = \rho (z_1 + z_2) "not using g"  
W4_P = \rho g (0 + z_2) "ignoring z_1"

**1-121** The atmospheric pressures at the top and the bottom of a building are read by a barometer to be 96.0 and 98.0 kPa. If the density of air is 1.0 kg/m^3, the height of the building is

(a) 17 m  
(b) 20 m  
(c) 170 m  
(d) 204 m  
(e) 252 m

*Answer* (d) 204 m

**Solution** Solved by EES Software. Solutions can be verified by copying-and-pasting the following lines on a blank EES screen. (Similar problems and their solutions can be obtained easily by modifying numerical values).

\[
\begin{align*}
\rho &= 1.0 \text{ kg/m}^3 \\
g &= 9.81 \text{ m/s}^2 \\
P_1 &= 96 \text{ kPa} \\
P_2 &= 98 \text{ kPa} \\
\Delta P &= P_2 - P_1 \text{ kPa} \\
\Delta P &= \rho g h / 1000 \text{ kPa}
\end{align*}
\]

"Some Wrong Solutions with Common Mistakes:"  
\Delta P = \rho g W_1_h / 1000 "not using g"  
\Delta P = g W_2_h / 1000 "not using rho"  
P_2 = \rho g W_3_h / 1000 "ignoring P_1"  
P_1 = \rho g W_4_h / 1000 "ignoring P_2"
1-122 An apple loses 4.5 kJ of heat as it cools per °C drop in its temperature. The amount of heat loss from the apple per °F drop in its temperature is
(a) 1.25 kJ  (b) 2.50 kJ  (c) 5.0 kJ  (d) 8.1 kJ  (e) 4.1 kJ

*Answer*  (b) 2.50 kJ

*Solution* Solved by EES Software. Solutions can be verified by copying-and-pasting the following lines on a blank EES screen. (Similar problems and their solutions can be obtained easily by modifying numerical values).

\[ Q_{\text{perC}} = 4.5 \text{ kJ} \]
\[ Q_{\text{perF}} = \frac{Q_{\text{perC}}}{1.8} \text{ kJ} \]

"Some Wrong Solutions with Common Mistakes:"
W1 \( Q = Q_{\text{perC}} \times 1.8 \) "multiplying instead of dividing"
W2 \( Q = Q_{\text{perC}} \) "setting them equal to each other"

1-123 Consider a 2-m deep swimming pool. The pressure difference between the top and bottom of the pool is
(a) 12.0 kPa  (b) 19.6 kPa  (c) 38.1 kPa  (d) 50.8 kPa  (e) 200 kPa

*Answer*  (b) 19.6 kPa

*Solution* Solved by EES Software. Solutions can be verified by copying-and-pasting the following lines on a blank EES screen. (Similar problems and their solutions can be obtained easily by modifying numerical values).

\[ \rho = 1000 \text{ kg/m}^3 \]
\[ g = 9.81 \text{ m/s}^2 \]
\[ z_1 = 0 \text{ m} \]
\[ z_2 = 2 \text{ m} \]
\[ \Delta P = \rho g (z_2 - z_1) / 1000 \text{ kPa} \]

"Some Wrong Solutions with Common Mistakes:"
W1 \( P = \rho (z_1 + z_2) / 1000 \) "not using g"
W2 \( P = \rho g (z_2 - z_1) / 2000 \) "taking half of z"
W3 \( P = \rho g (z_2 - z_1) \) "not dividing by 1000"
1-124 At sea level, the weight of a 1 kg mass in SI units is 9.81 N. The weight of a 1 lbm mass in English units is
(a) 1 lbf  (b) 9.81 lbf  (c) 32.2 lbf  (d) 0.1 lbf  (e) 0.031 lbf

*Answer*  (a) 1 lbf

*Solution* Solved by EES Software. Solutions can be verified by copying-and-pasting the following lines on a blank EES screen. (Similar problems and their solutions can be obtained easily by modifying numerical values).

\[
m=1 \text{ "lbm"} \\
g=32.2 \text{ "ft/s}^2" \\
W=m*g/32.2 \text{ "lbf"}
\]

"Some Wrong Solutions with Common Mistakes:"
\[
g_{\text{SI}}=9.81 \text{ "m/s}^2" \\
W_1=W=m*g_{\text{SI}} \text{ "Using wrong conversion"} \\
W_2=W=m*g \text{ "Using wrong conversion"} \\
W_3=W=m/g_{\text{SI}} \text{ "Using wrong conversion"} \\
W_4=W=m/g \text{ "Using wrong conversion"}
\]

1-125 During a heating process, the temperature of an object rises by 20°C. This temperature rise is equivalent to a temperature rise of
(a) 20°F  (b) 52°F  (c) 36 K  (d) 36 R  (e) 293 K

*Answer*  (d) 36 R

*Solution* Solved by EES Software. Solutions can be verified by copying-and-pasting the following lines on a blank EES screen. (Similar problems and their solutions can be obtained easily by modifying numerical values).

\[
T_{\text{inC}}=20 \text{ "C"} \\
T_{\text{inR}}=T_{\text{inC}}*1.8 \text{ "R"}
\]

"Some Wrong Solutions with Common Mistakes:"
\[
W_1=T_{\text{inF}}=T_{\text{inC}} \text{ "F, setting C and F equal to each other"} \\
W_2=T_{\text{inF}}=T_{\text{inC}}*1.8+32 \text{ "F, converting to F"} \\
W_3=T_{\text{inK}}=1.8*T_{\text{inC}} \text{ "K, wrong conversion from C to K"} \\
W_4=T_{\text{inK}}=T_{\text{inC}}+273 \text{ "K, converting to K"}
\]